Quantum information processing, quantum communication and quantum Artificial Intelligence in semiconductor quantum computer

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New Scientist,23.09.2019: Google claims it has finally reached quantum supremacy

"Google's quantum processor tackled a random sampling problem ... Although one of its qubits didn't work, the remaining 53 were quantum entangled with one another and used to generate a set of binary digits and check their distribution was truly random. The paper calculates the task would have taken Summit, the world's best supercomputer, 10.000 years - but Sycamore did it in 3 minutes and 20 seconds."



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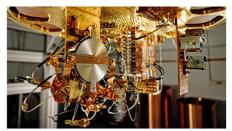
ALL TOPICS

1166 1

NEWS QUANTUM PHO

Rumors hint that Google has accomplished quantum supremacy

Reports suggest a quantum computer has surpassed standard computers on a specific type of calculation



Joogle may have created the first quantum computer that can perform a calculation impossible on classical computers. A dilution refrigerator (shown) is used to good quantum processors.

Source: https://www.sciencenews.org/article/rumors-hint-that-google-has-accomplishedquantum-supremacy

IBM: the future is quantum

https://www.ibm.com/quantum-computing/

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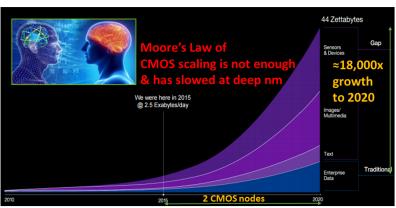
IBM 50Q System: a cryostat wired for a 50 qubit system.

Source:

https://www.ibm.com/blogs/research/2017/11/the-future-is-quantum/



Why Quantum Computing?



- Cognitive computing (see T.J.Watson presentation @ GTC2016)
- Machine learning will dominate the compute infrastructure

Bits and Qubits

Classical bit:

0 or 1

Coin on table



Digital: self-correcting

Quantum bit:

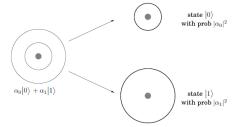
 $\psi = \cos\theta |0\rangle + \sin\theta e^{i\phi} |1\rangle$

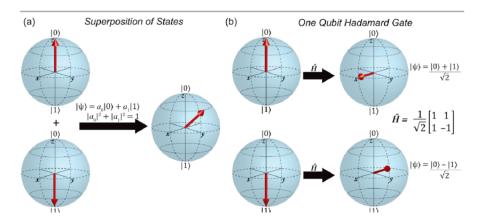
Coin in space



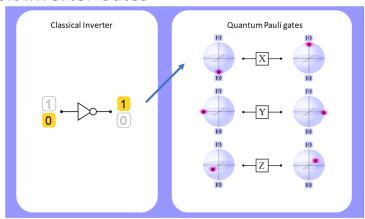
Analog: sensitive to small errors

Measurement of a superposition has the effect of forcing the system to decide on a particular state, with probabilities determined by the amplitudes.





Qubit Inverter Gates



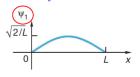
Interpreting the wavefunction

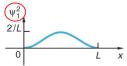
• Probability interpretation

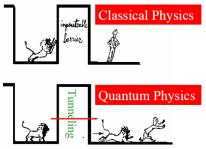
The square magnitude of the wavefunction $|\Psi|^2$ gives the probability of finding the particle at a particular spatial location



 $Probability = (Wavefunction)^2$







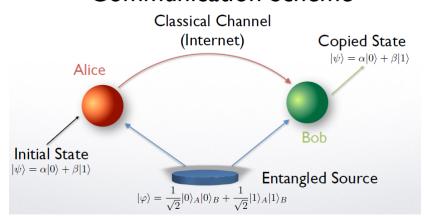
The difference between classical theory and quantum theory, illustrating tunneling through potential barrier. This illustration was used by Van Vleck in his last publication, the Julian E. Mack Lecture at his Alma Mater, the University of Wisconsin, in 1979. (Affer B. Bleaney, Contemp. Phys. 25 (1984) 320.)

Quantum mechanics vs Neural Networks

Quantum mechanics	Neural Networks
wave function	neuron
Superposition (coherence)	interconnections (weights)
Measurement (decoherence)	evolution to attractor
Entanglement	learning rule
unitary transformations	gain function (transformation)

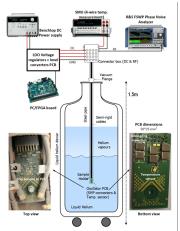
Quantum neural networks by A.Ezhov and Dan Ventura

Communication Scheme

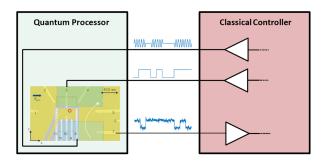


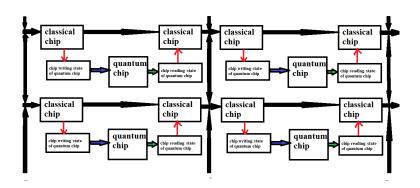
Measurement Setup





Current Quantum Computers





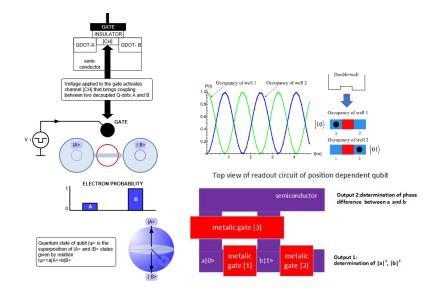
Overview

- Desired features for programmable quantum electronics
- 2 Anticorrelation principle in semiconductor and in superconducting electronics
- Quantum gates
- 4 Two types of position dependent qubits
- 5 Physical properties of coupled Single Electron Lines
- 6 Interface between semiconductor and superconducting quantum computer
- Hybrid q-semiconductor and q-superconducting computer
 - Analogies between Cooper pair box and CMOS qbit
- Quantum logic
 - Q-Chemistry
 - Q-Communication
 - Q-Artificial Neural Network
 - Q-Al and Q-ALife



Main desired features of quantum programmable electronics

- Smooth interface between classical and quantum circuits
- High integration and high logical density
- Desired operational temperature above 1K
- Electrical writting up the qubits states
- Electrical reading up of qubits states
- Electrical way of entangling two particles
- Smooth transition from classical to quantum regime

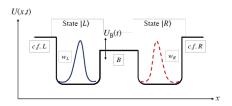


Electrostatic qubit by Panagiotis et al [IEEE Open Access, 2019], Pomorski et al. [Spie 2019], Fujisawa [2004]

Position based qubit in tight binding model

The Hamiltonian of this system is given as

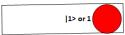
$$\hat{H}(t) = \begin{pmatrix} E_{p1}(t) & t_{s12}(t) \\ t_{s12}^{\dagger}(t) & E_{p2}(t) \end{pmatrix}_{[x=(x_1,x_2)]} =
= (E_1(t) |E_1\rangle_t \langle E_1|_t + E_2(t) |E_2\rangle \langle E_2|_{[E=(E_1,E_2)]}.$$
(1)



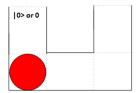
Classical/Logic circuits from electron-electron anticorrelation



Classical / Quantum Swap gate



Input of CNOT gate



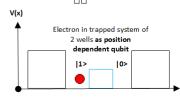
Control bit or qubit for CNOT gate



Quantum Swap Gate or CNOT

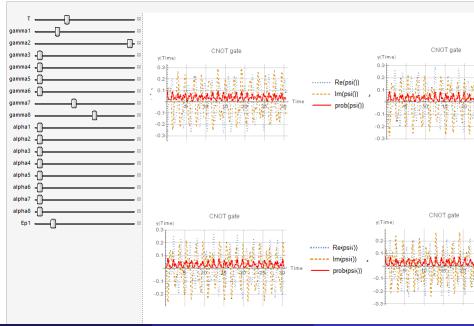


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Output of Swap Gate/ CNOT gate

Information is diffused between 2 wells so |\psi = a|0> + b |1>



Occupancy ocillations in position based qubit at nodes 1 and 2

$$P_{1}(t) = |\alpha(t)|^{2} = \frac{1}{2}((|\alpha(0)|^{2} + |\beta(0)|^{2}) + \frac{1}{2}(|\alpha(0)|^{2} - |\beta(0)|^{2})\cos((\frac{E_{2} - E_{1})t}{\hbar})) = \cos(\Theta(t))^{2},$$

$$P_{2}(t) = |\alpha(t)|^{2} = \frac{1}{2}((|\alpha(0)|^{2} + |\beta(0)|^{2}) - \frac{1}{2}(|\alpha(0)|^{2} - |\beta(0)|^{2})\cos((\frac{E_{2} - E_{1})t}{\hbar})) = \sin(\Theta(t))^{2},$$
(2)

and it oscillates periodically with frequency proportional to distance between energetic levels E_2 and E_1 and is given as $\omega_0 = \frac{E_2 - E_1}{\hbar}$.

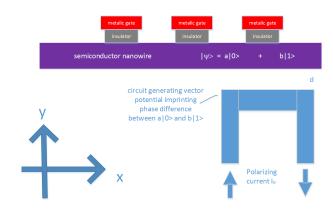
Bloch sphere dynamics for position based qubit

$$-\sin(\phi(t)) = \left[\frac{\sin(\frac{E_1t}{\hbar})(|\alpha(0)|^2-|\beta(0)|^2)+\sin(\frac{E_2t}{\hbar})(|\alpha(0)|^2+|\beta(0)|^2)}{\cos(\frac{E_1t}{\hbar})(|\alpha(0)|^2-|\beta(0)|^2)+\cos(\frac{E_2t}{\hbar})(|\alpha(0)|^2+|\beta(0)|^2)}\right] =$$

$$\frac{(1-e^{-i\frac{2E_1t}{\hbar}})(|\alpha(0)|^2-|\beta(0)|^2)+\left(\frac{\cos(\Theta(t))^2-\frac{1}{2}}{\frac{1}{2}(|\alpha(0)|^2-|\beta(0)|^2)}+i|\sqrt{1-(\frac{\cos(\Theta(t))^2-\frac{1}{2}}{\frac{1}{2}(|\alpha(0)|^2-|\beta(0)|^2)})^2}|-e^{-i\frac{(E_2+E_1)t}{\hbar}}\right)}{i(1+e^{-i\frac{2E_1t}{\hbar}}))(|\alpha(0)|^2-|\beta(0)|^2)+i\left(\frac{\cos(\Theta(t))^2-\frac{1}{2}}{\frac{1}{2}(|\alpha(0)|^2-|\beta(0)|^2)}+i|\sqrt{1-(\frac{\cos(\Theta(t))^2-\frac{1}{2}}{\frac{1}{2}(|\alpha(0)|^2-|\beta(0)|^2)})^2}|+e^{-i\frac{(E_1+E_2)t}{\hbar}}\right)}$$

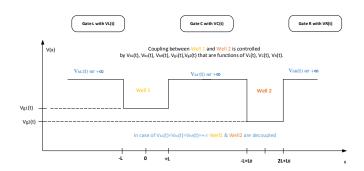
Coevolution of both Θ and ϕ on Bloch sphere.

Phase rotating gate

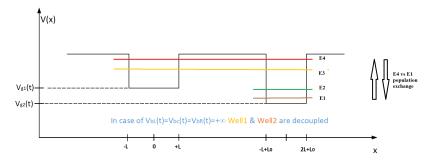


Effective potential in piece-wise approximation and electric Aharonov-Bohm effect (phase rotation gate)

Wavefunction phase difference across 2 deep wells controlled electrostatically is $\propto \frac{-1}{\hbar} \int_{t_0}^t (V_{g_1}(t') - V_{g_2}(t'))) dt'$.



Localized vs delocalized state in system of coupled q-dots



AC field allows for the transition of the delocalized state into localized state and reversely !!!

Two types of position based qubits

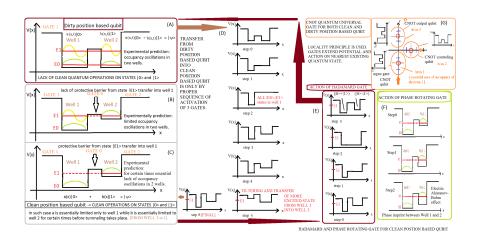
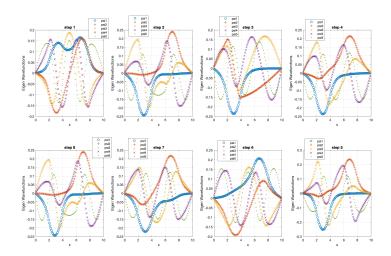


Figure: [Pomorski et al, Spie 2019]

Transition between two types of position based qubits



Problem of 2 electrostatically interacting particles in perturbative limit

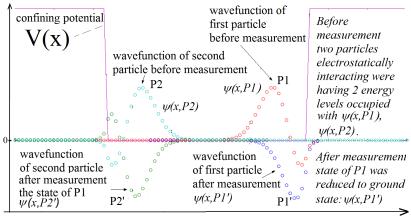
In the case of 2 weakly interacting particles we have $\psi(x_A, x_B, t) = \psi(x_A, t)\psi(x_B, t)$ what gives

$$[-\frac{\hbar^2}{2m}\frac{d^2}{dx_A^2} + \lambda \frac{\int_{-\infty}^{+\infty} e^2 \psi_B(x,t) \psi_B^{\dagger}(x,t) dx}{4\pi\epsilon_0 |x_A - x|} + V_A(x_A)]\psi_A(x_A,t) =$$

$$= E_A \psi_A(x_A,t) \qquad (3)$$

$$[-\frac{\hbar^{2}}{2m}\frac{d^{2}}{dx_{B}^{2}} + \lambda \frac{\int_{-\infty}^{+\infty} e^{2}\psi_{A}(x,t)\psi_{A}^{\dagger}(x,t)dx}{4\pi\epsilon_{0}|x_{B}-x|} + V_{B}(x_{B})]\psi_{B}(x_{B},t) = E_{B}(t)\psi_{B}(x_{B},t).$$
(4)

Case of 2 electrons in single quantum well



2 particles in rectangular well with electrostatic interaction

LETTER TO THE EDITOR

Spontaneous magnetic flux and quantum noise in an annular mesoscopic SND junction

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Physics and Astronomy Department, The University of British Columbia, 6224 Agricultural Road, Vancouver, BC, V6T 1Z1, Canada

Received 4 November 1997

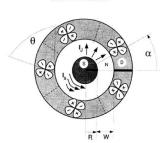


Figure 1. Annular SND junction. The c-axis of the d-wave superconductor is chosen to be parallel to the SD boundary; θ is the angle between the SD boundary and the nodal plane of the d-wave order parameter ($\theta \in \theta \le \pi/2$).

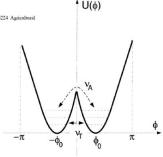
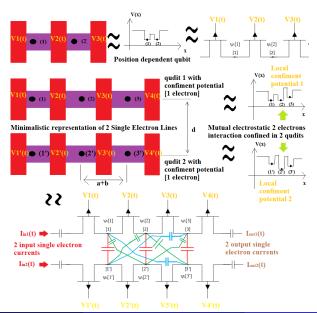


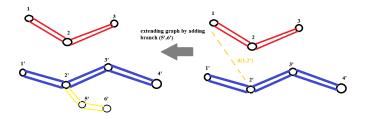
Figure 2. Effective potential and transition rates for the phase vinuction.

Most features present in superconducting nanostructures are presented in single electron CMOS technology!!!

Case of 2 electrostatically coupled Single Electron Lines

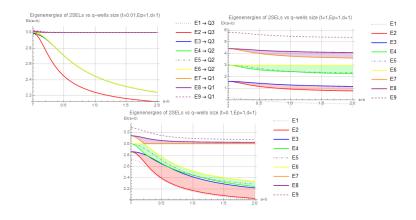


Electrostatically controlled topology of graphs of coupled q-dots in chain of semiconductor q-dots



In semiconductor one observes the anticorrelation of electrons positions due to electrostatic repulsion and minimization of electrostatic field energy. In superconductor one observes the anticorrelation of electric non-dissipative currents due to magnetic field shielding. There is charge-phase duality in anticorrelation!!!

Programmable band structure in chain of coupled q-dots

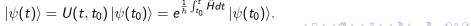


Analytical tight-binding approach for coupled q-dots

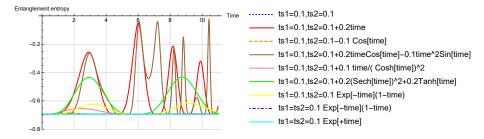
$$\hat{H}(t) = \begin{pmatrix} 2E_{\rho}(t) + \frac{q^2}{d_1} & t_{sr2}(t) & t_{sr1}(t) & 0 \\ t_{sr2}(t) & 2E_{\rho}(t) + \frac{q^2}{\sqrt{(d_1)^2 + (b+a)^2}} & 0 & t_{sr1}(t) \\ t_{sr1}(t) & 0 & 2E_{\rho}(t) + \frac{q^2}{\sqrt{(d_1)^2 + (b+a)^2}} & t_{sr2}(t) \\ 0 & t_{sr1}(t) & t_{sr2}(t) & 2E_{\rho}(t) + \frac{q^2}{d_1} \end{pmatrix} = \\ = \hat{\sigma}_0 \times \hat{\sigma}_0 q_{11} + \hat{\sigma}_3 \times \hat{\sigma}_3 q_{22} + t_{sr2}(t) \hat{\sigma}_0 \times \hat{\sigma}_3 + t_{sr1}(t) \hat{\sigma}_3 \times \hat{\sigma}_0$$

that has only real value components $H_{k,l}$ with

that has only real value components
$$H_{k,l}$$
 with $q_{11} = E_p(t) + \frac{E_{c1} + E_{c2}}{2} = E_p(t) + \frac{1}{2}(\frac{q^2}{d_1} + \frac{q^2}{\sqrt{(d_1)^2 + (b+a)^2}}),$ $q_{22} = \frac{E_{c1} - E_{c2}}{2} = \frac{1}{2}(\frac{q^2}{d_1} - \frac{q^2}{\sqrt{(d_1)^2 + (b+a)^2}}) \text{ and } Q_{11}(t) = \int_{t_0}^t dt' q_{11}(t'),$ $Q_{22}(t) = \int_{t_0}^t dt' q_{22}(t'), \ TR1(t) = \int_{t_0}^t dt' t_{sr1}(t'), \ TR2(t) = \int_{t_0}^t dt' t_{sr2}(t').$ $S_B(t) = Tr[\rho_B(t)Log[\rho_B(t)]]$ (5)



Entanglement entropy of coupled qubits with time



Electrostatic control of entanglement is demonstrated by tight-binding model in symmetric Q-Swap gates when two hopping constants are the same at initial state and when the state is initially in the ground state.

Correlation function

$$C(E_{c1} - E_{c2}) = \frac{q^2}{d} - \frac{q^2}{\sqrt{d^2 + (a+b)^2}}, t_{s1}, t_{s2}, p_{E1}, p_{E2}, p_{E3}, p_{E4}, \phi_{E10}, \phi_{E20}, \phi_{E30}, \phi_{E40}, t) =$$

$$= \frac{N_{+,+} + N_{-,-} - N_{-,+} - N_{+,-}}{N_{+,+} + N_{-,-} + N_{-,+} + N_{+,-}} =$$

$$4\left[\frac{\sqrt{p_{E1}}\sqrt{p_{E2}}(t_{s1} - t_{s2})\cos[-t\sqrt{(E_{c1} - E_{c2})^2 + 4(t_{s1} - t_{s2})^2} + \phi_{E10} - \phi_{E20}\right]}{\sqrt{(E_{c1} - E_{c2})^2 + 4(t_{s1} - t_{s2})^2}} + \frac{\sqrt{p_{E3}}\sqrt{p_{E4}}(t_{s1} + t_{s2})\cos[-t\sqrt{(E_{c1} - E_{c2})^2 + 4(t_{s1} + t_{s2})^2} + \phi_{E30} - \phi_{E40}]}{\sqrt{(E_{c1} - E_{c2})^2 + 4(t_{s1} + t_{s2})^2}} - (E_{c1} - E_{c2})\left[\frac{p_{E1} - p_{E2}}{\sqrt{(E_{c1} - E_{c2})^2 + 4(t_{s1} + t_{s2})^2}} + \frac{p_{E3} - p_{E4}}{\sqrt{(E_{c1} - E_{c2})^2 + 4(t_{s1} + t_{s2})^2}}\right]$$

$$(6)$$

We are going to use Jaynes-Cumming Hamiltonian [?] that describes the interactiton atom with cavity by means of electromagnetic field. In the simplest approach the cavity Hamiltonian describing waveguide without dissipation is represented as

$$H_{cavity} = \hbar \omega_c (\frac{1}{2} + \hat{a}^{\dagger} \hat{a}),$$
 (7)

where \hat{a}^{\dagger} (\hat{a}) is the photon creation (annihilation) operator and number of photons in cavity is given as $n=\hat{a}^{\dagger}\hat{a}$. At the same we can represent the two level qubit system

$$H_{qubit} = E_g |g\rangle \langle g| + E_e |e\rangle \langle e|.$$
 (8)

The interaction Hamilonian is of the following form

$$H_{qubit-cavity} = g(\hat{a}^{\dagger}\sigma_{-} + \hat{a}\sigma_{+}), \tag{9}$$

where $\sigma_- = \sigma_1 - i\sigma_2$, $\sigma_+ = \sigma_1 + i\sigma_2$. The qubity-cavity interaction has the electric-dipole nature so quasiclassically we can write

$$H_{qubit-cavity} = \hat{d} \cdot \hat{E} = g(\sigma_- + \sigma_+)(\hat{a} + \hat{a}^{\dagger}) \approx g(\hat{a}^{\dagger}\sigma_- + \hat{a}\sigma_+).$$
 (10)

Here we have neglected the terms $g(\sigma_-\hat{a} + \sigma_+\hat{a}^\dagger)$ and our approach is known as rotating phase

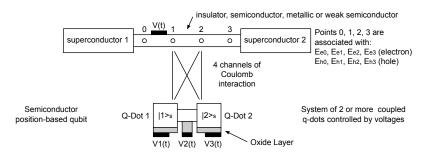
During photon emission from qubit the energy level is lowered and reversely during photon absorption the energy level of qubit is raised what is seen in the term $\hat{a}\sigma_+$. The system Hamiltonian is given as $H=H_{cavity}+H_{qubit}+H_{qubit-cavity}.$ It is not hard to construct the Hilbert space for Jaynes-Cumming Hamiltonian. Essentially we are considering the tensor product of qubit space and cavity space.

$$|\psi\rangle = \gamma_{1} |\phi_{1}\rangle |0\rangle + \gamma_{2} |\phi_{1}\rangle |1\rangle + \gamma_{3} |\phi_{2}\rangle |0\rangle + \gamma_{4} |\phi_{2}\rangle |1\rangle =$$

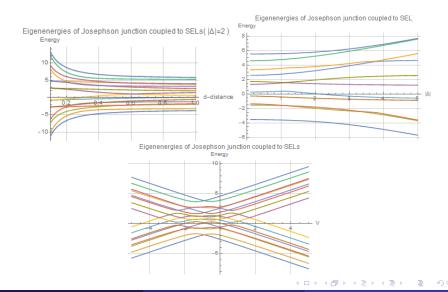
$$\begin{pmatrix} \gamma_{1} \\ \gamma_{2} \\ \gamma_{3} \\ \gamma_{4} \end{pmatrix}, 1 = \langle \psi |\psi\rangle = |\gamma_{1}|^{2} + ... + |\gamma_{4}|^{2}. \tag{11}$$

Electrostatic interface between semiconductor and superconducting qubit

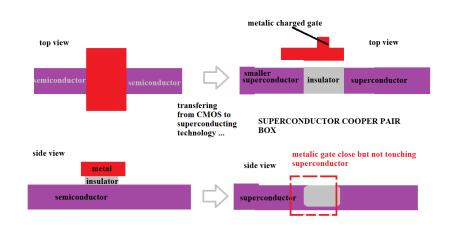
Josephson Junction interacting with two coupled Q-Dots semiconductor qubits



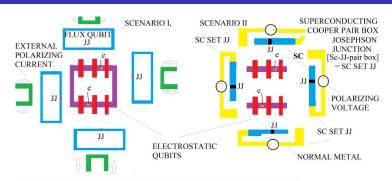
Tight-binding model in description of JJs coupled to semiconductor qubit and modification of ABS in JJ



Electrostatically controlled superconducting and semiconducting qubits



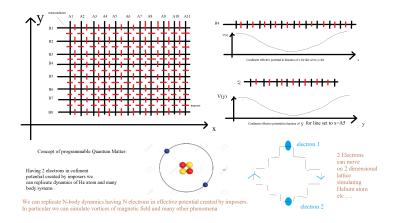
Electromagnetic interface between semiconductor and superconducting circuits



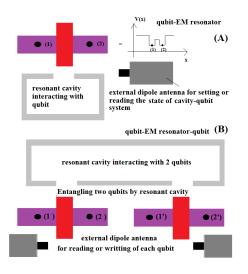
INTERFACE BETWEEN SUPERCONDUCTOR AND SEMICONDUCTOR QUBITS

[K.Pomorski, P.Giounanlis, E.Blokhina, D.Leipold, P.Peczkowski, Robert Bogdan Staszewski, From two types of electrostatic position-dependent semiconductor qubits to quantum universal gates and hybrid semiconductor-superconducting quantum computer, Proc. SPIE 11054, 2019]

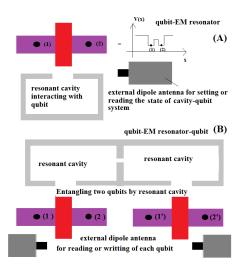
Quantum chemistry in semiconductor lattices



Quantum Communication

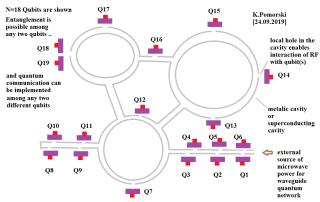


Quantum Communication over Long Line

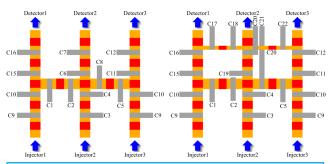


Quantum Internet

Concept of quantum internet implemented in position based qubits with use of waveguides of any topology



Quantum Neural Network

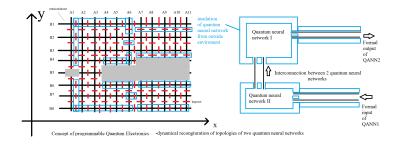


Concept of quantum and classical single electron neural network in CMOS. It can mimic all quantum universal gates. It can be controlled with voltages applied to Cl., Cl. 22, gates, Additionally one can use external magnetic field to control its performance.

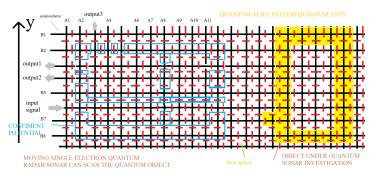
by Krzysztof Pomorski, 16 Nov 2018

Q-Neural Network can mimic any physical system of N bodies.

Reconfigurable Quantum Neural Networks



Quantum chemistry in semiconductor lattices

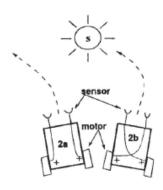


SINGLE ELECTRON RADAR CAN BE RECOGNIZED AS QUANTUM AGENT OR QUANTUM ANT HAVING SENSOR AND QUANTUM SONAR IT CAN BE BASED ON NON-UNIFORM ELECTRIC OR MAGNETIC FIELD AS WELL AS CONGLOMERATION OF OTHER CHARGED PARTICLES CAPTURED BY CONFIMENT POTENTIAL (YELLOW)

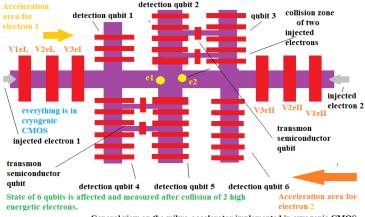
ALL CONFIMENT POTENTIALS CAN BE CONTROLLED EXTERNALLY BY FINITE STATE MACHINE [BLUE+YELLOW]

PROPER OPERATION OF QUANTUM AGENTS REQUIRES CONSTANT FLOW OF ELECTRONS AS INPUT SIGNAL AND CONSTANT ANALYSIS OF OUTPUT SIGNALS.

Braitenberg vehices



Quantum accelerator

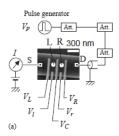


General view on the mikro-accelerator implemented in cryogenic CMOS [Krzysztof Pomorski]

Various experiements can be conducted for various energies of colliding electrons.

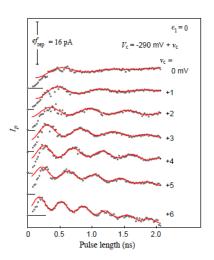
Measurement of electron entangled state after collision can be attempted.

Previous experiments



T. Fujisawa et al. / Physica E 21 (2004) 1046-1052

The DQDs used in this work are defined by metal gates on top of a GaAs/AlGaAs heterostructure with a two-dimensional electron gas (2DEG). Each dot contains about 25 electrons with on-site charging energy $E_{\rm c} \sim 1.3$ meV. The interdot charging energy is $U=200~{\rm \mu eV}$. The qubit parameters, ε and Λ , and tunneling rates, $\Gamma_{\rm L}$ and $\Gamma_{\rm R}$, respectively, for left and right



Acknowledgments

All requirements for implementation of large scale Quantum Computer are to be fulfilled.

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New company: Quantum Hardware Systems (QHS)

http://www.quantumhardwaresystems.com/ Mission: Linking existing quantum and classical old and new technologies in realistic fashion ...

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The End